

## Boyton Primary School Calculation Policy 2024-2025

This policy supports the White Rose maths scheme used throughout the school. Progression within each area of calculation is in line with the programme of study in the 2014 National Curriculum. This calculation policy should be used to support children to develop a deep understanding of number and calculation. This policy has been designed to teach children through the use of concrete, pictorial and abstract representations.

- Concrete representation— a pupil is first introduced to an idea or skill by acting it out with real objects. This is a 'hands on' component using real objects and is a foundation for conceptual understanding.
- Pictorial representation a pupil has sufficiently understood the 'hands on' experiences performed and can now relate them to representations, such as a diagram or picture of the problem.
- Abstract representation—a pupil is now capable of representing problems by using mathematical notation, for example 12 x 2 = 24. It is important that conceptual understanding, supported by the use of representation, is secure for all procedures. Reinforcement is achieved by going back and forth between these representations.

### Mathematics Mastery

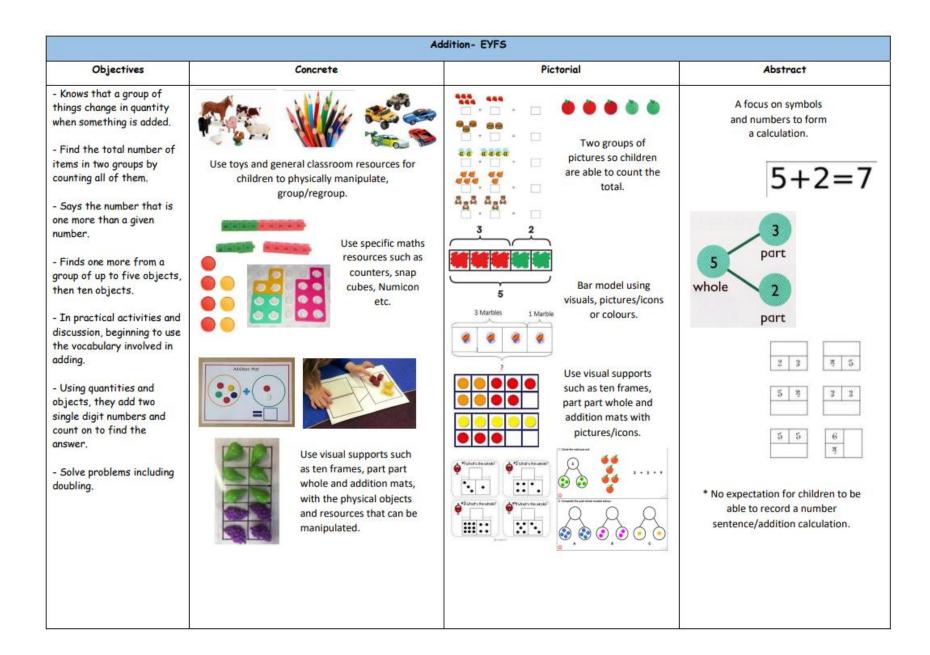
At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures through the use of concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in Year 1 to Year 6 in line with the requirements of the 2014 Primary National Curriculum.

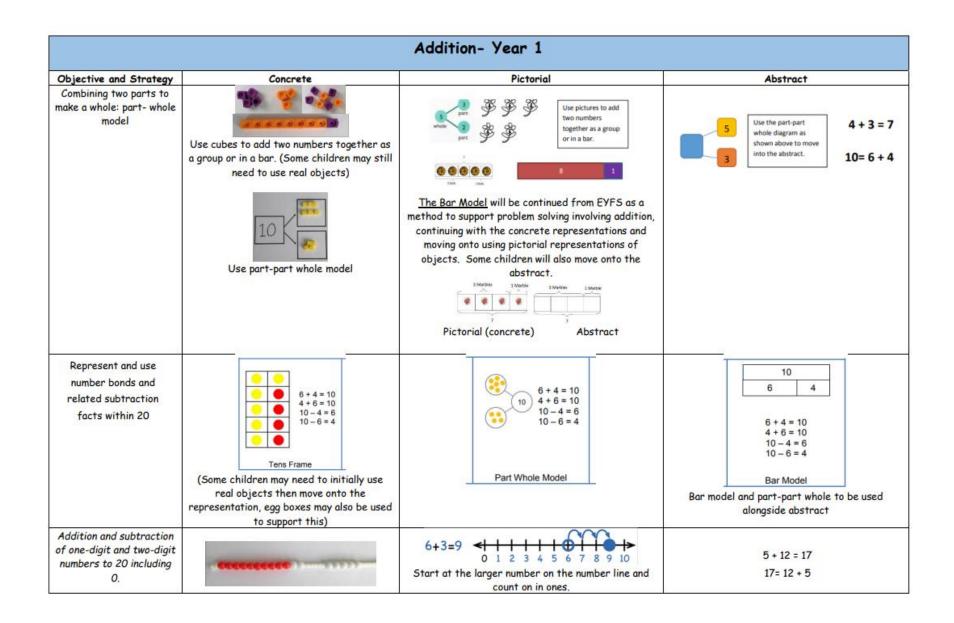
### How to use the policy:

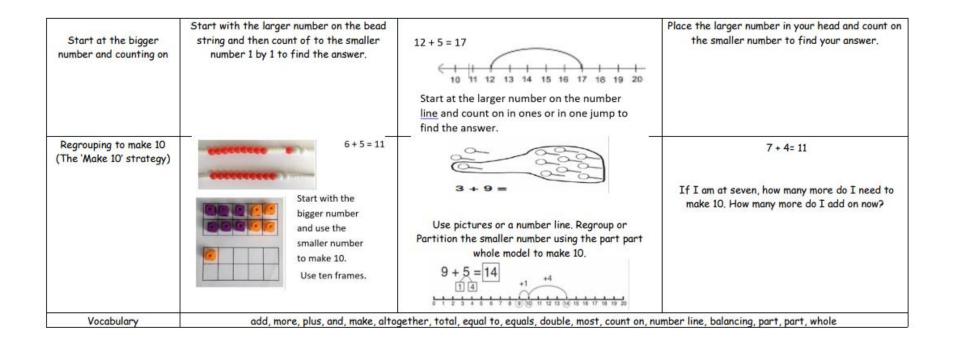
This mathematics policy is a guide for all staff in Boyton Primary and has been adapted from work by the NCETM. All teachers have been given the scheme of work from the White Rose Maths Hub and are required to base their planning around their year group's modules and not to move onto a higher year group's scheme work. These modules use the Singapore Maths Methods and are affiliated to the workings of the 2014 Maths Programme of Study. Teachers can use any teaching resources that they wish to use and the policy does not recommend one set of resources over another, rather that, a variety of resources are used.

For each of the four rules of number, different strategies are laid out, together with examples of what concrete materials can be used and how, along with suggested pictorial representations. The principle of the concrete-pictorial-abstract (CPA) approach [Make it, Draw it, Write it] is for children to have a true understanding of a mathematical concept, they need to master all three phases within a year group's scheme of work.

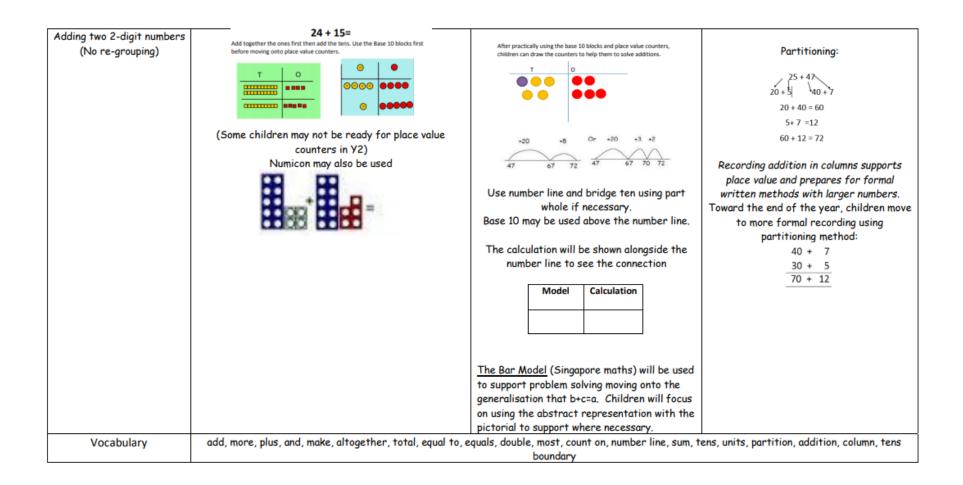
## Addition

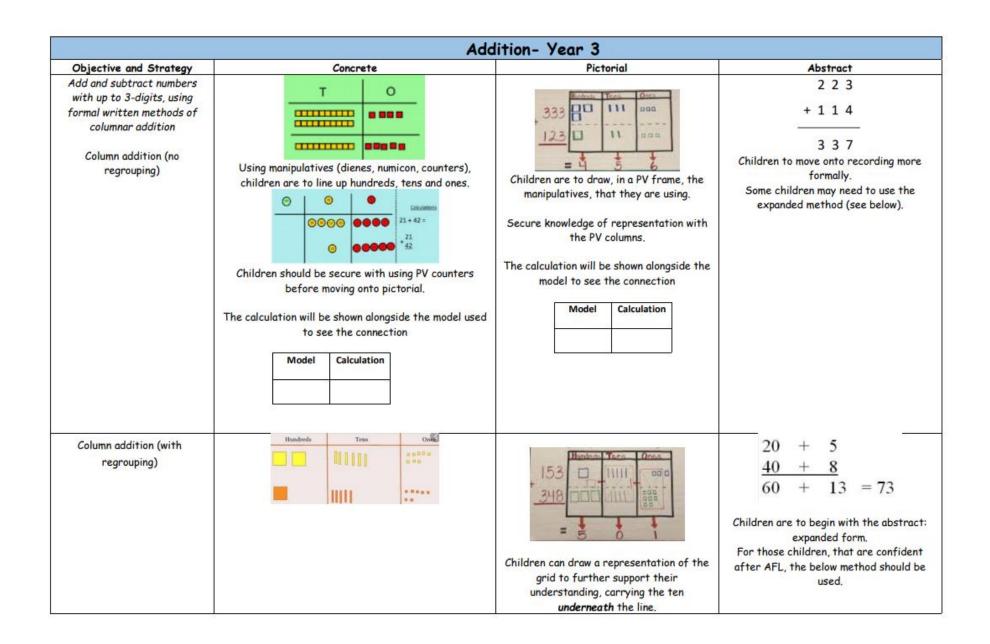




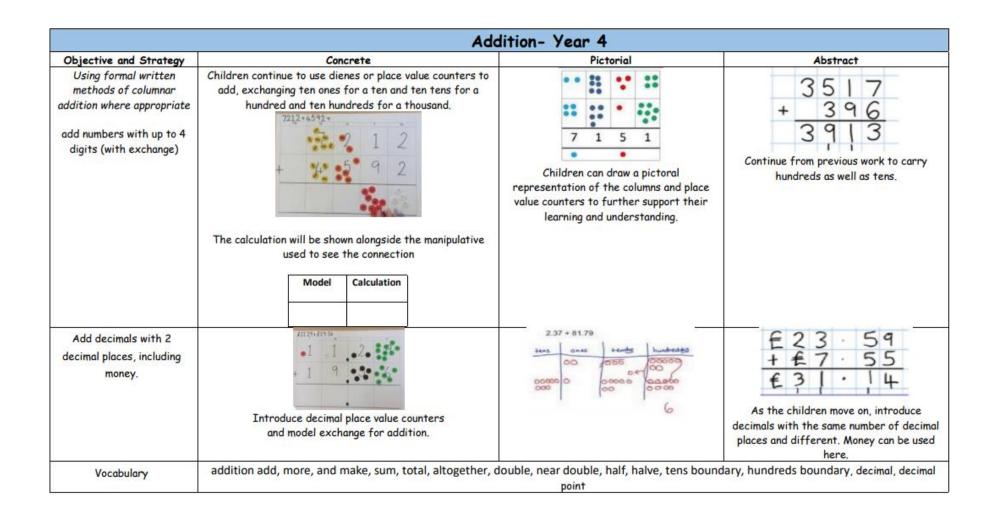


Addition- Year 2				
Objective and Strategy	Concrete	Pictorial	Abstract	
Adding 3 1-digit numbers	4 + 7 + 6= 17         Put 4 and 6 together to make 10. Add on 7.         Following on from making 10, make 10 with 2 of the digits (if possible) then add on the third digit.	Add together three groups of objects. Draw a picture to recombine the groups to make 10.	$\underbrace{4}_{10} + 7 + 6 = 10 + 7$ = 10 $= 17$ Combine the two numbers that make 10 and then add on the remainder.	
Adding a 2-digit number			17 + 5 = 22	
and ones	Image: 17 + 5 = 22      Image: 17 + 5 = 32	17 + 5 = 22 Use part part whole and number line to model. 10 + 7 $10 + 7$	Explore related facts 17 + 5 = 22 5 + 17 = 22 22 - 17 = 5 22 - 5 = 17 22	
Adding a 2-digit number and multiples of 10	25 + 10 = 35 Explore that the ones digit does not change	27 + 30 +10 +10 +10 27 37 47 57 Base 10 may be used above the number line initially. The calculation will be shown alongside the number line to see the connection	27 + 10 = 37 27 + 20 = 47 27 + 0 = 57	





	127 + 115 = 242 Exchange ten ones for a ten. Model using Dienes, Numicon and place value counters.	$ \begin{array}{r} 536 \\ + 85 \\ \underline{621} \\ 11 \end{array} $
/ocabulary	addition add, more, and make, sum, total, altogether, double, near double, hal	f, halve, tens boundary, hundreds boundary

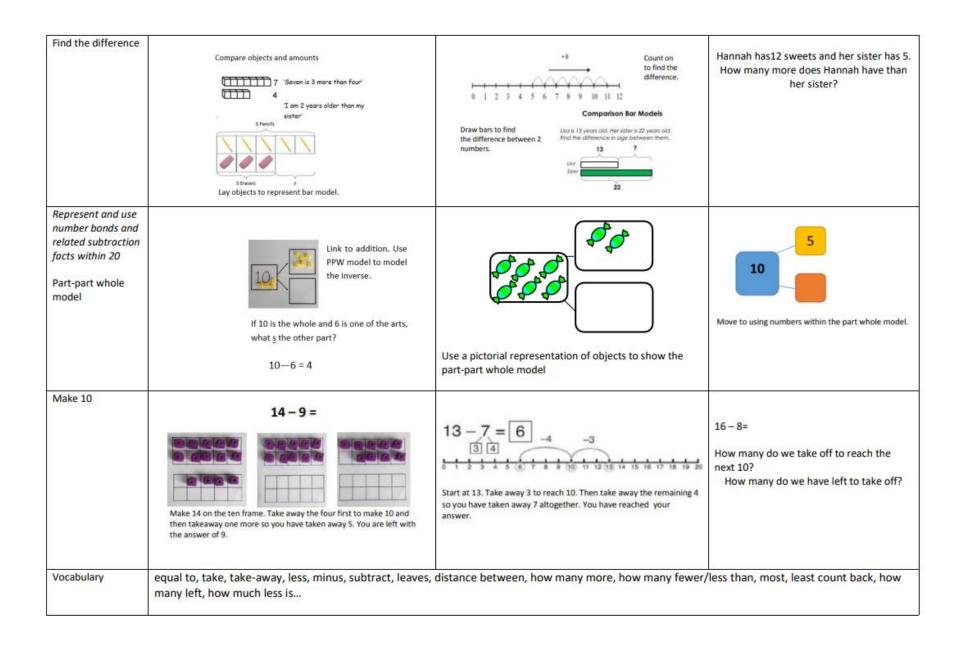


	Addition	- Year 5/6	
Objective and Strategy	Concrete	Pictorial	Abstract
add numbers with more than 4 digits.	See Year 4	See Year 4	
			Children should have abstract supported by a pictorial or concrete if needed.
add several numbers of increasing complexity, including adding money, measure and decimals with different numbers of decimal points.	See Year 4	See Year 4	$ \begin{array}{r} 8 & 1, 0 & 5 & 9 \\ 3 & 6 & 6 & 8 \\ 1 & 5, 3 & 0 & 1 \\ + & 2 & 0, 5 & 5 & 1 \\ 1 & 2 & 0, 5 & 7 & 9 \\ + & 2 & 0, 5 & 7 & 9 \\ 1 & 2 & 0, 5 & 7 & 9 \\ \hline 2 & 3 & 0 & 3 & 6 & 1 \\ 9 & 0 & 8 & 0 \\ 5 & 9 & 7 & 7 & 0 \\ + & 1 & 3 & 0 & 0 \\ \hline 9 & 3 & 5 & 1 & 1 \\ \hline \end{array} $ Insert zeros for place holders.
/ocabulary a	addition add, more, and make, sum, total, alto	gether, double, near double, half, halve decimal point	· · · · · · · · · · · · · · · · · · ·

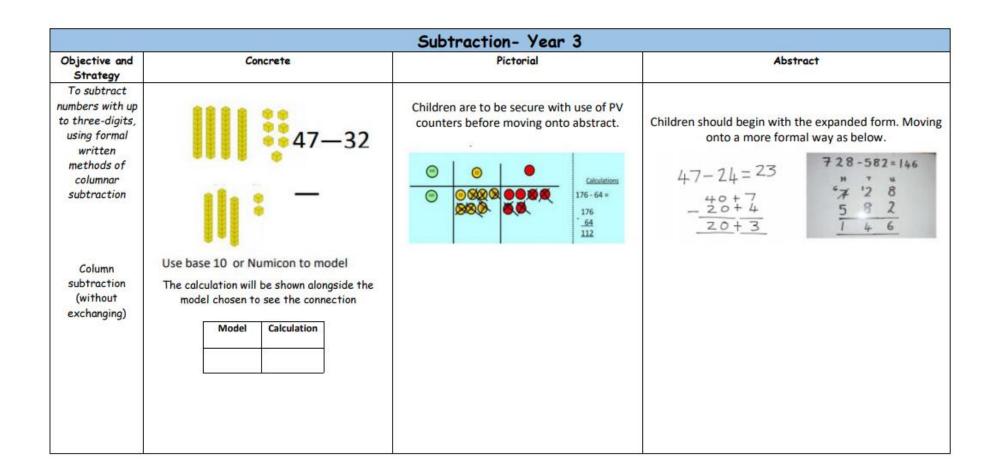
Subtraction

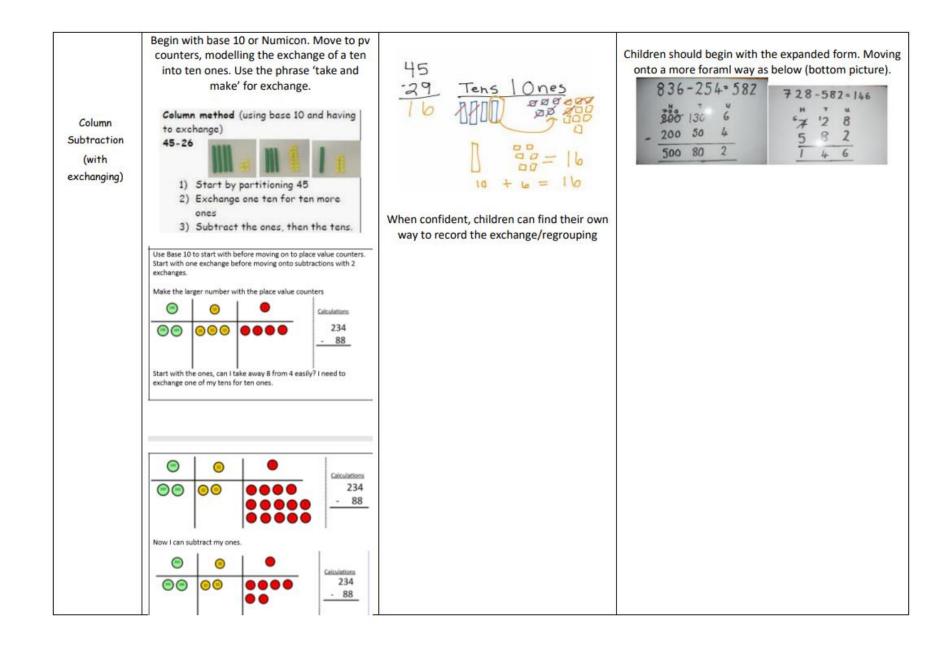
Subtraction- EYFS			
Objectives Concrete Pictorial		Pictorial	Abstract
<ul> <li>Knows that a group of things change in quantity when something is taken away</li> <li>Find one less from a group of five objects, then ten objects.</li> <li>In practical activities and discussion, beginning to use the vocabulary involved in subtracting.</li> <li>Using quantities and objects, they subtract two single digit numbers and count back to find the answer.</li> </ul>	<image/>	A group of pictures for children to cross out or cover quantities to support subtraction.	A focus on symbols and numbers to form a calculation. 10-1=? $10-6=4$ $3 ?$ $7$ $7-3=?$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $7$ $3$ $3$ $7$ $7$ $3$ $3$ $7$ $3$ $3$ $7$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$ $3$

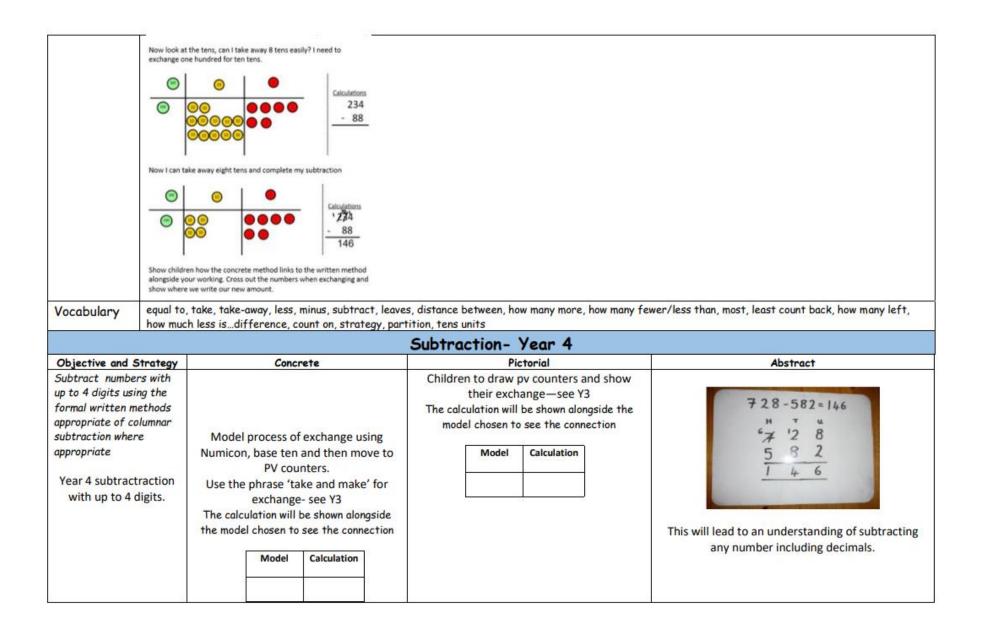
Objective and Strategy	Concrete	Pictorial	Abstract
Subtract one-digit and two-digit numbers to 20, including 0. Taking away ones	Use physical objects, <u>counters</u> , cubes <u>etc</u> to show how objects can be taken away. 6-4 = 2 4-2 = 2	Cross out drawn objects to show what has been taken away. $ \begin{array}{c}                                     $	7—4 = 3 16—9 = 7
Counting back	Make the larger number in your subtraction. Move the beads along your bead string as you count backwards in ones. 13 - 4 Use counters and move them away from the group as you take then away counting backwards as you go.	$\begin{array}{c} -1 & -1 \\ \hline & 5 & -3 & = 2 \\ \hline & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 \\ \hline \\ $	Put 13 in your head, count back 4. What number are you at? (Use your fingers to he you)

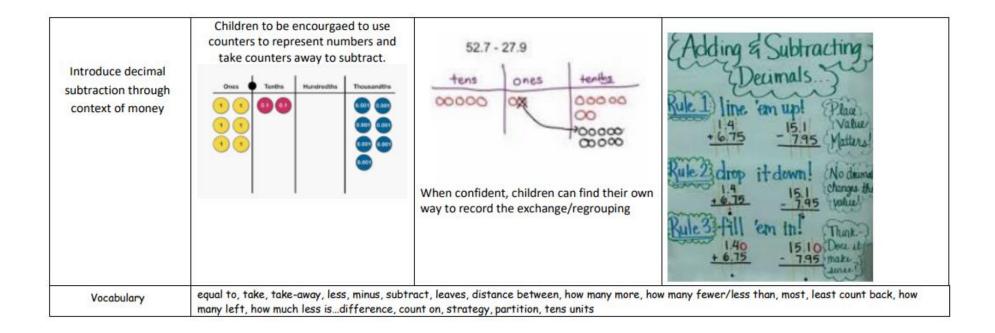


	Subtraction- Year 2				
Objective and Strategy	Concrete	Pictorial	Abstract		
Subtract a two-digit number and ones, a two- digit number and tens, two two-digit numbers Partitioning to subtract without re- Grouping: 'Friendly numbers'	34-13 = 21       Image: Constraint of the second seco	Children draw representations of Dienes and cross off.	43—21 = 22 Recording subtraction in columns supports place value and prepares for formal written methods with larger numbers. Toward the end of the year, children move to more formal recording using partitioning method: e.g. 43-21=22 40 and 3 <u>-20 and 1</u> <u>20 and 2</u>		
Make ten strategy	34-28 Use a bead bar or bead strings to model counting to next ten and the rest.	4 76 80 90 93 'counting on' to find 'difference' Use a number line to count on to next ten and then the rest.	93—76 = 17		
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, di left, how much less	stance between, how many more, how many fewer, s isdifference, count on, strategy, partition, tens			





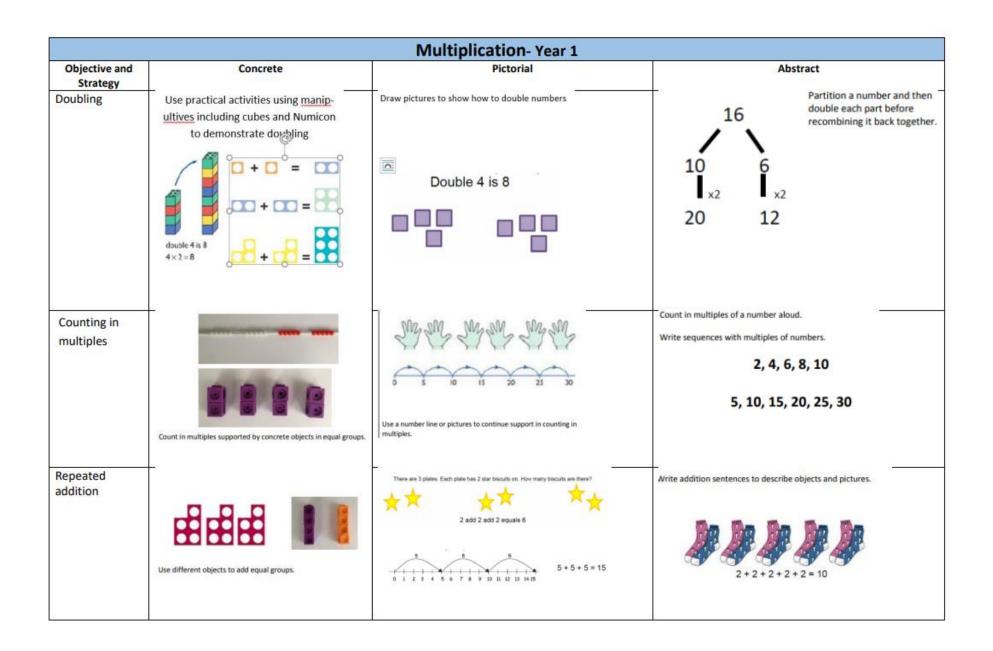




Subtraction- Year 5/6				
Objective and Strategy	Concrete	Pictorial	Abstract	
Subtract with at least 4 digits, including money and measures. Subtract with increasingly large and more complex numbers and decimal values (up to 3 decimal place).	See Year 4	See Year 4	$\begin{array}{c} 37 & 8 & 0 & 6 & 9 \\ - & 8 & 9 & 9 & 4 & 9 \\ \hline & 6 & 0 & 7 & 5 & 0 \\ \hline 37 & 9 & 5 & 34 & 1 & 9 & kg \\ - & 36 & 0 & 8 & 0 & kg \\ \hline & 6 & 9 & 3 & 3 & 9 & kg \end{array}$	
Vocabulary	equal to, take, take-away, less, minus, subtract, leaves, di left, how much less isdifference, count on, strategy, par		any fewer/less than, most, least count back, how many	

# Multiplication

		Multiplication-EYFS	
Objectives	Concrete	Pictorial	Abstract
- Solve problems	a series and a series of the s	What is double 4?	1+1= 7+7=
including doubling			2+2= 8+8=
			3+3= 9+9=
			4+4= 10+10=
		4 + 4 = 8	5+5= 11+11=
	Counting an	d other	6+6= 12+12=
	2       4       6       8       10       make 2 equa groups.         2       4       6       8       10       make 2 equa groups.         Physical ar life exam that enco children t concep doubling adding t equal groups.	Pictures and icons that encourage children to see concept of doubling as adding two equal groups. adding two equal groups. adding two equal groups.	adding two equal groups.



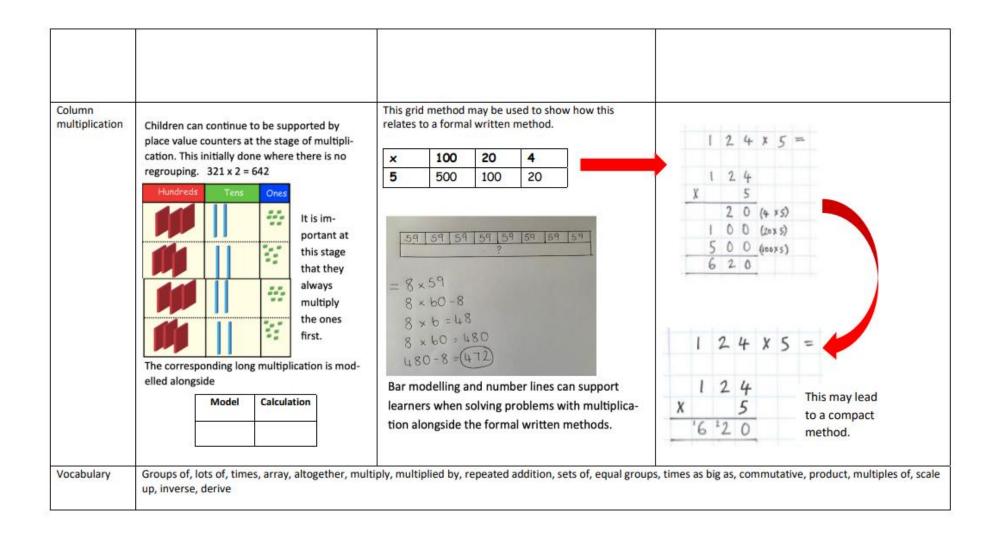
		Use pictorial including number lines to solve problemshere are 3 sweets in one bag. How many sweets are in 5 bags altogether? 3+3+3+3+3 = 15 0 0 0 0 0 0 0 0 0 0 0 0 0	
Understanding arrays	Use objects laid out in arrays to find the answers to 2 lots 5, 3 lots of 2 etc.		3 x 2 = 6 2 x 5 = 10
Vocabulary	Groups of, lots of, times, array, altogether, mu	ultiply	Į

		Multiplication-Year 2	
Objective and Strategy	Concrete	Pictorial	Abstract
Counting in multiples of 2, 3, 4, 5, 10 from 0 (repeated addition)	Count the groups as children are skip counting, children may use their fin- gers as they are skip counting. Use bar models. 5+5+5+5+5+5+5=40	Number lines, counting sticks and bar models should be used to show repre- sentation of counting in multiples.	Count in multiples of a number aloud. Write sequences with multiples of numbers. 0, 2, 4, 6, 8, 10 0, 3, 6, 9, 12, 15 0, 5, 10, 15, 20, 25 , 30
Multiplication is commutative	Create arrays using counters and cu- bes and Numicon.	Use representations of arrays to show different calculations and explore commutativity.	$4 \times 3 =$ $12 = 3 \times 4$ $12 = 4 \times 3$ Use an array to write multiplication sentences and reinforce repeated addition. $0 = 0 = 0$ $5 + 5 + 5 = 15$ $3 + 3 + 3 + 3 + 3 = 15$ $5 \times 3 = 15$ $3 \times 5 = 15$

Using the nverse This should be aught alongside division, so bupils earn how they work alongside each other.		$ \begin{array}{c} 8\\ 4\\ 2\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $	2 x 4 = 8 4 x 2 = 8 8 + 2 = 4 8 + 4 = 2 8 = 2 x 4 8 = 4 x 2 2 = 8 + 4 4 = 8 $\div$ 2 Show all 8 related fact family sentences.
/ocabulary	Groups of, lots of, times, array, altogethe	er, multiply, multiplied by, repeated addition, s	ets of, equal groups, times as big as, commutative.

		Multiplication-Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Multiplying two digit number by a one digit number Grid method progressing to the formal method. Solving problems including missing number problems, integer scaling problems.	Show the link with arrays to first introduce the grid method.         Image: Show the link with arrays to first introduce the grid method.         Image: Show the link with arrays to first introduce the grid method.         Image: Show the link with arrays to first introduce the grid method.         Image: Show the link with arrays to first introduce the grid method.         Image: Show the link with arrays to first introduce the grid method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 to move towards a more compact method.         Image: Show to using Base 10 towards a more compact method.	Children can represent their work with place value counters in a way that they understand. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below. $\boxed{\begin{array}{c} 4 + x & 3 = 72 \\ \hline 4 & 0 & 0 \\ \hline 0 0 $	Start with multiplying by one digit numbers and showing the clear addition alongside the grid. TO x O I       9       3       5       4         X       I       0       8       3       3       2       4         Start with multiplying by one digit numbers and showing the clear addition alongside the grid.       I       9       X       3       5       4         Y       I       0       g       3       3       0       2       4         Children to add up each column to find the answer.       I
	The calculation will be shown alongside the model chosen to see the connection	4	
	Model Calculation		
Vocabulary	Groups of, lots of, times, array, altogether, mu scale up	I Itiply, multiplied by, repeated addition, sets of, equal	groups, times as big as, commutative, product, multiples of

Objective and	Concrete Pictorial		Abstract	
Strategy				
Multiply two- digit and three-digit numbers by a one-digit number using formal written layout		Children can represent their work with place value counters in a way that they understand. They can draw the counters using colours to show different amounts or just use the circles in the different columns to show their thinking as shown below.	HTO x O $1 \ 3 \ 5 \ x \ 5 = 6 \ 7 \ 5$ $x \ 1 \ 0 \ 0 \ 3 \ 0 \ 5$ $5 \ 5 \ 0 \ 0 \ 1 \ 5 \ 0 \ 2 \ 5$	
Grid method recap from year 3 for 2 digits x 1 digit Multiplying numbers by 1	Move on to place value counters to show how we are finding groups of a number. We are multiplying by 4 so we need 4 rows.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Children to add up each column to find the answer.	
digit (year 4 expectation)	Add up each column, starting with the ones making any exchanges needed.			



Multiplication Year 5					
Objective and Strategy	Concrete	Pictorial	Abstract		
Multiply numbers up to 4-digits by a one-digit number using the format written method, including long multiplication for 2-digit numbers Column multiplication for 3 and 4 digits x 1 digit	Children can continue to be supported by place value counters at the stage of multipli- cation. This initially done where there is no regrouping. 321 x 2 = 642	×         300         20         7           4         1200         80         28	$327 \\ x 4 \\ 28 \\ 80 \\ 1200 \\ 1308 \\ \hline 3 2 7 \\ x 4 \\ 1 3 0 8 \\ 1 2 \\ \hline 1 3 0 8 \\ 1 2 \\ \hline 1 2 $		
Column multiplication (long multiplication)	Manipulatives may still be used with the corresponding long multiplication modelled alongside           Model         Calculation	Moving forward, multiply by a 2 digit number showing the different rows within the grid method. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	24 x 6 on the first row. (6 x 4 = 24, carrying the 2 4 x 1 6 1 4 4 2 4 0 3 8 4 2 4 x 10 on the second row. Show multiplying by 10 by putting zero in the units first. 1 2 3 4 1 3 4 1 3 3 4 1 3 4		
Vocabulary		multiply, multiplied by, repeated addition, sets of, e pr pairs, composite numbers, prime number, factors	equal groups, times as big as, commutative, product, , squared, cubed		

Objective and	Concrete	Pictorial	Abstract	
Strategy				
Multiply			Remind children that the single digit belongs	
decimal up to			in the units column. Line up the decimal	
2 decimal			points in the question and the answer.	
place by a				
single digit.				
			3 · 1 9	
			× 8	
			25.52	
vocabulary Grou	Groups of, lots of, times, array, altogether, multiply, multiplied by, repeated addition, sets of, equal groups, times as big as, commutative, product, multiples of, scale up, inverse, derive, factor pairs, composite numbers, prime number, factors, squared, cubed			

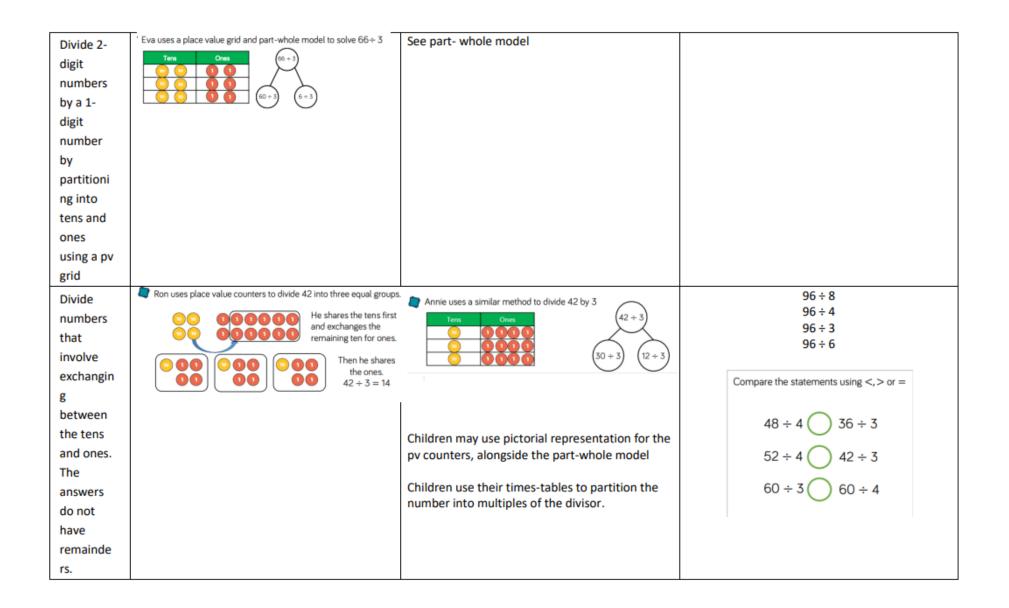
Division

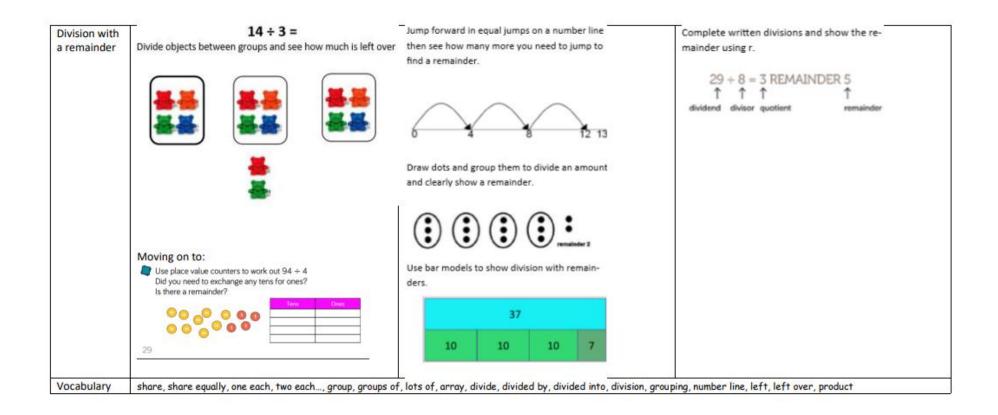
Division- EYFS						
Objectives	Concrete	Pictorial	Abstract			
<ul> <li>Solve problems including halving and sharing.</li> <li>Halving a whole, halving a quantity of objects.</li> <li>Sharing a quantity of objects.</li> </ul>	Image: state of the state	Image: Second state of the second s				

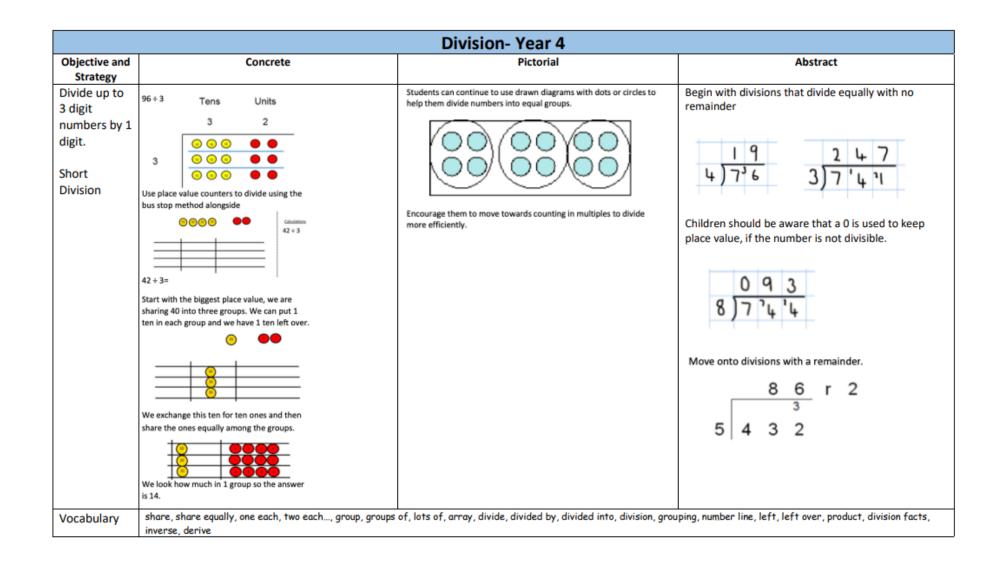
Objective and Strategy	Concrete	Distantal	
		Pictorial	Abstract
Division as sharing (sharing objects into groups)	Image: Non-State State	Children use pictures or shapes to share quantities. Children use pictures or shapes to share quantities. $3 \Rightarrow 3 \Rightarrow$	Share 9 buns between three people. 9 ÷ 3 = 3
		12	
		000 000 000 000	
		12 ÷ 4 = 3	

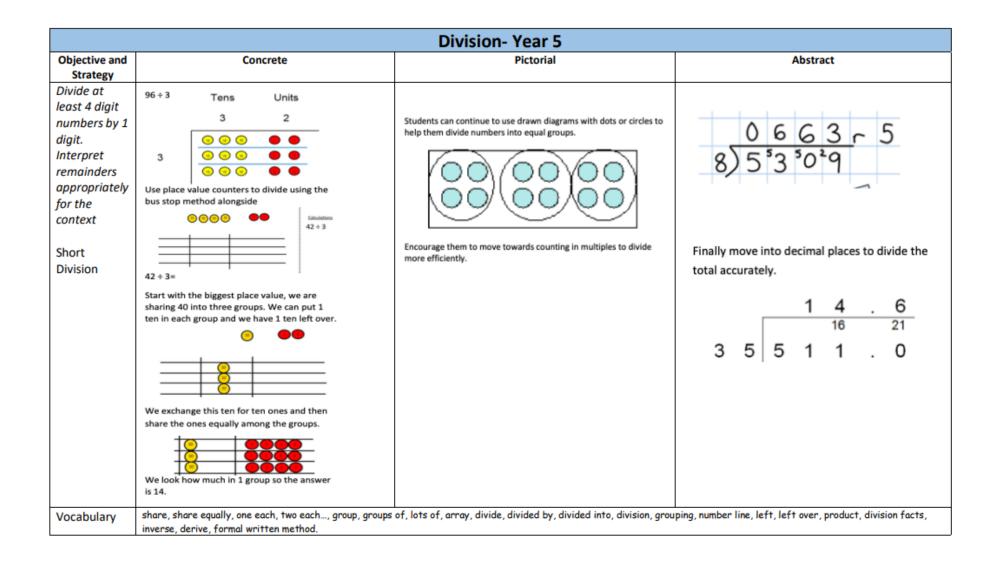
Division as grouping $U_{3}$ understanding. $U_{3}$ counters, objects or place value counters to aid understanding. 0 + 3 = 32 0	Objective and Strategy	Concrete	Pictorial	Abstract
*		understanding.	0 1 2 3 4 5 6 7 8 9 10 11 12 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3 3	Divide 28 into 7 groups. How many are in

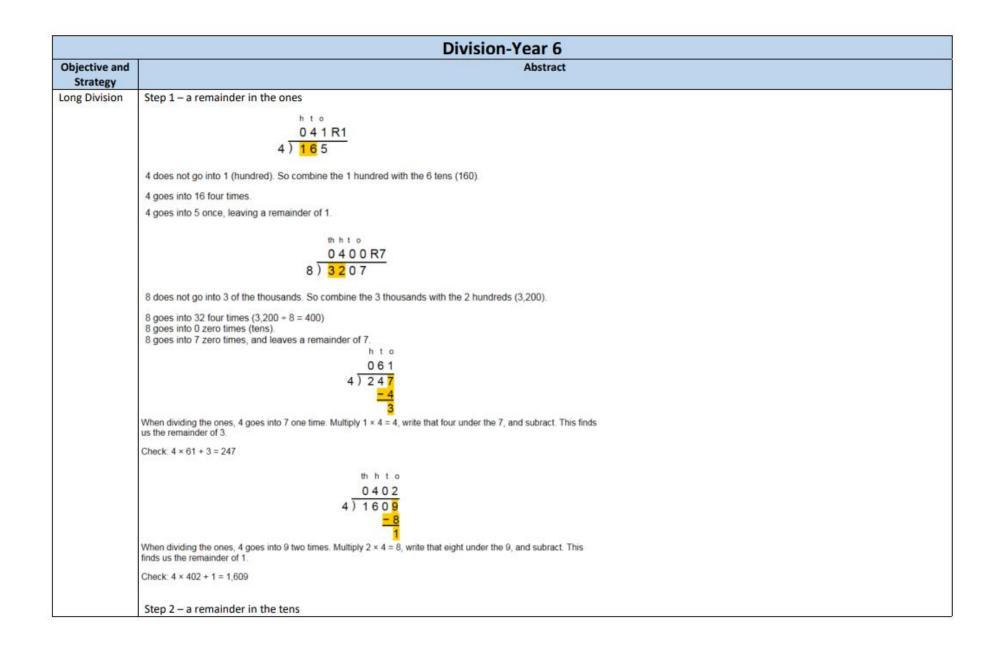
		Division- Year 3	
Objective and Strategy	Concrete	Pictorial	Abstract
Division as grouping	Use cubes, counters, objects or place value counters to aid understanding.	Continue to use bar modelling to aid solving division problems.	How many groups of 6 in 24?
	24 divided into groups of $6 = 4$ 96 + 3 = 32	20 ? 20 ÷ 5 = ? 5 x ? = 20	24 ÷ 6 = 4
Division with arrays	Link division to multiplication by creating an array and thinking about the number sentences that can be created. Eg 15 ÷ 3 = 5 5 x 3 = 15 15 ÷ 5 = 3 3 x 5 = 15	Draw an array and use lines to split the array into groups to make multiplication and division sentences	Find the inverse of multiplication and division sentences by creating eight linking number sentences. 7 x 4 = 28 4 x 7 = 28 28 ÷ 7 = 4 28 ÷ 4 = 7 28 = 7 x 4 28 = 4 x 7 4 = 28 ÷ 7 7 = 28 ÷ 4



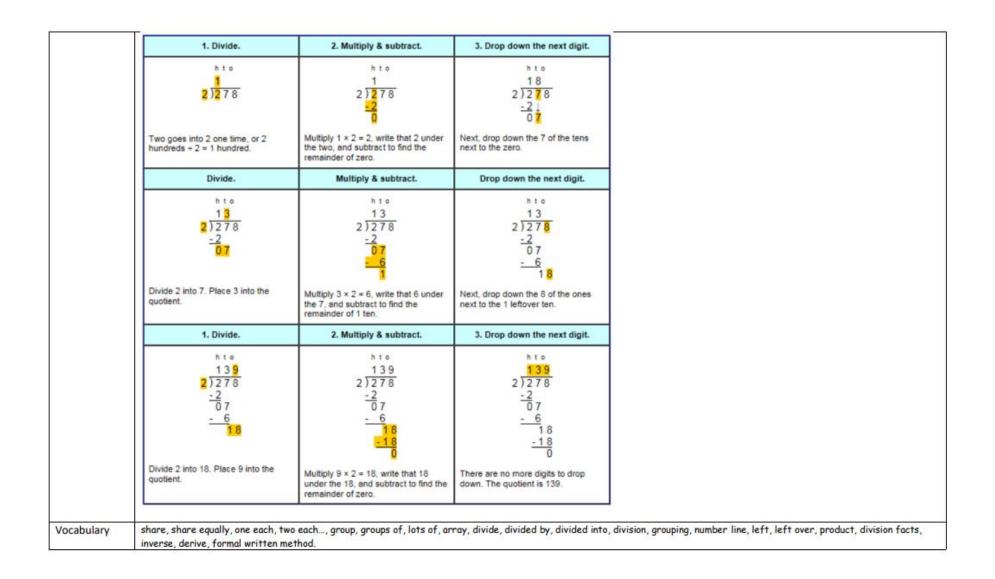








1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
2) <mark>5</mark> 8	2 2) <u>5</u> 8 <u>-4</u> 1	29 $2)58$ $-41$ $18$
Two goes into 5 two times, or 5 te + 2 = 2 whole tens but there is remainder!		Next, drop down the 8 of the ones next to the leftover 1 ten. You combine the remainder ten with 8 ones, and get 18.
1. Divide.	2. Multiply & subtract.	3. Drop down the next digit.
29 2)58 -4 18	t o 2 9 2 ) 5 8 - 4 - 1 8 0	$2) \frac{29}{18} - \frac{4}{18} - \frac{18}{0}$
Divide 2 into 18. Place 9 into the quotient.	Multiply 9 × 2 = 18, write that 18 under the 18, and subtract.	The division is over since there are no more digits in the dividend. The



## Minimal Resources required to support the CPA approach (depending on year group):

- 10 frames (including egg boxes)
- Straws/pipe cleaners Bead strings (to 20 and 100)
- Rekenrek frames Base 10/Dienes (including magnetic to model on flip chart)
- Place value grids
- Double-sided counters
- Part-part whole templates
- Place value counters (KS2)
- Multi-link cubes